

Ex Tetrad

arg1- arg2- recessive to WT mutants

- Type 1 1 Arg⁺ 3 Arg⁻ (T)
 - Type 2 4 Arg⁺ (PD)
- highly linked case

AB = aB = Tetatype
 AB = AB
 Ab = Ab

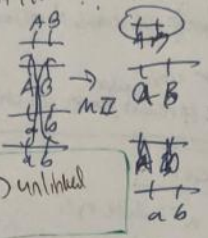
$$Dist = \frac{\#T \cdot 100 \cdot M}{2 \cdot \#total}$$

ab
 ab
 AB
 AB
 - Nonparental d. type

arg3- x arg1- - arg3, dom to WT

Type 1	2	3
1 Arg ⁺ 3 Arg ⁻	4 Arg ⁺	2 Arg ⁺
T	PD	2 Arg ⁻
		NPD

COMPLEMENTATION TEST
 USEFUL ONLY w/ RECESSIVE MUTATIONS !!



1:4:1 ratio, PD:T:NPD => unlinked

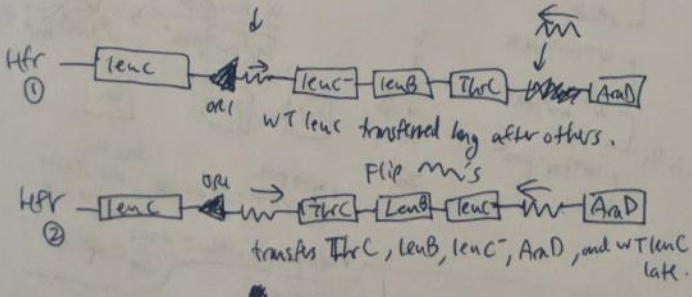
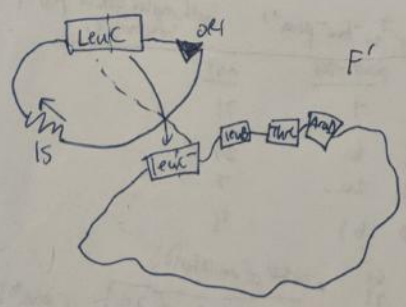
wildly linked: $Dist = 100 \cdot \frac{T + 6 \cdot NPD}{2 \cdot Total}$

tightly linked - only T, PD

$$\chi^2 = \sum \frac{(o-e)^2}{e}$$

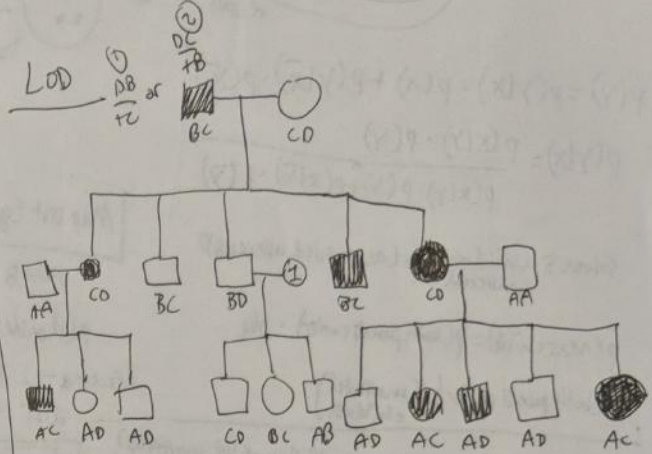
all phenotypic classes

χ^2 0.016 0.46
 p 0.9 0.5
 can't reject null hypothesis



Use multiploid (hfr ①) to make w/ double mutants. # of WT phenotypes suggests order of genes.

4 mutants = P
 3:1 mutants T
 2:2 Mutab - NPD



- autosomal dominant
- 1 must be AC
- cannot be completely linked as in

LOD score - second gen $\theta = 0.08$

$$Log = \log \left[\frac{\theta^R \cdot (1-\theta)^{NR}}{0.5^{Tot}} \right]$$

$$LOD = \log_{10} \left[\frac{1}{2} \left(\frac{\theta^R \cdot (1-\theta)^{NR}}{0.5^T} \right)^{Phase 1} + \frac{1}{2} \left(\frac{\theta^R \cdot (1-\theta)^{NR}}{0.5^T} \right)^{Phase 2} \right]$$

R=4 NR=1

R=1 NR=4

LOD = -0.038

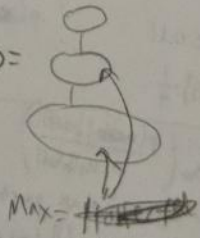
3rd gen LOD - we know phases of parent.

$$LOD = \log_{10} \left[\frac{\theta^1 \cdot (1-\theta)^3}{0.5^T} \right] = 1.06$$

- middle is uninformative

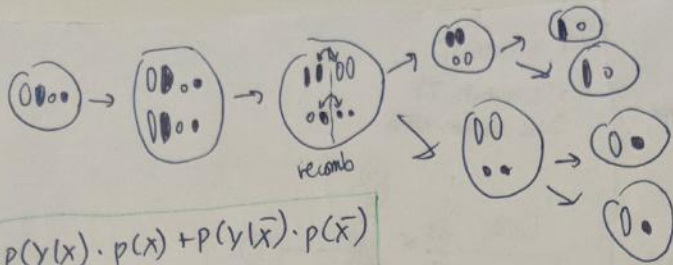
Total = 1.022

Simple LOD =



Max = ~~1.022~~

A offspring 0.3 - 0.3



- unlinked: #parentals = #recombs
- weakly linked: #parentals > #recombs
- tightly linked: #parentals >>> #recombs

Look at recombination tests with heterozygotes and cross of WT or recessive homozygote
- Look at combos of gametes to form dihybrids

$$P(Y) = P(Y|X) \cdot P(X) + P(Y|\bar{X}) \cdot P(\bar{X})$$

$$P(Y|X) = \frac{P(X|Y) \cdot P(Y)}{P(X|Y) \cdot P(Y) + P(\bar{X}|Y) \cdot P(Y)}$$

Given 5 children unaffected, p(next child affected)?

$$p(\text{next child}) = p(\text{both parents carrier}) \cdot \frac{1}{4}$$

$$p(\text{both parents carrier} | 5 \text{ unaffected children})$$

Probability of both parents carriers if 1st child unaffected?

$$P(Y|X) = \dots$$

So $p(X|Y) = \text{Bayes}$ $p(X)$ calc'd
 $p(Y|\bar{X}) = \text{calc'd}$

$$\text{Map dist (genetic distance)} = 100 \cdot \frac{\# \text{recombs}}{\# \text{gametes}} \text{ (cM)}$$

$$A \leftrightarrow B \text{ } \frac{18}{100} \text{ cM} = p(\text{recomb}) = 0.18$$

$$p(\text{double recomb}) = p(\text{recomb A}) \cdot p(\text{recomb B})$$

3 factor cross \rightarrow 2 factor cross, double dist \rightarrow #recombs gametes which is $\frac{2 \cdot \# \text{double recombs}}{\text{Total}} \cdot 100$

3 Factor cross

w⁻: white eyes
bw⁻: bent wings
para^s: paralysis
X-linked recessive

$$P: \text{♂ } X + \frac{w^- bw^- para^s}{w^- bw^- para^s}$$

$$F1: \text{♂ } w^- bw^- para^s / y \quad \text{♀ } w^- bw^- para^s / WT X$$

• F1 Females will informative meioses b/c het.

• Cross F1 ♀ w/ ♂ w⁻ bw⁻ para^s ... both males/female progeny are informative.

	paralyzed	not
Normal eyes, wings	4	71
White eyes, normal wings	6	23
Normal eyes, bent wings	20	7
White eyes, bent wings	65	4

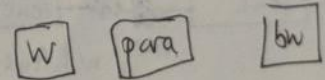
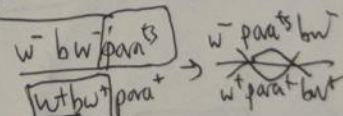
[w⁻ bw⁻ para^s / recip] 65 71

[w⁻ bw⁻ para^s / w⁻ bw⁻ para^s] 6 7

[w⁻ bw⁻ para^s / w⁻ bw⁻ para^s] 4 4

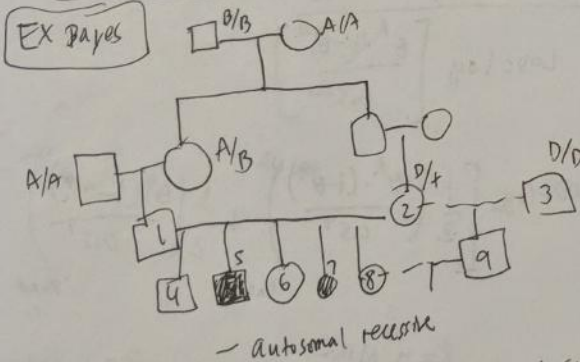
[w⁻ bw⁻ para^s / w⁻ bw⁻ para^s] 20 23

• order of mutations:



• w⁻ para^s bw⁻ $\# = 8 + 43 = \frac{51}{200} \cdot 100 \text{ cM}$

• w⁻ bw⁻ para^s $\# = 13 + 8 = \frac{21}{200} \cdot 100 \text{ cM}$



- autosomal recessive

1) given #3 not carrier \rightarrow 9 \rightarrow 1/2 prob carrier
8 \rightarrow 1 is D/+, 2 is D/+
so 8 can be D/D, D/+ or D/+.

$$\frac{2}{3}$$

2) #8 \leftrightarrow #9 5 unaffected children, next child affected?

$$p(\text{next affected}) = p(\text{carrier}) \cdot \frac{1}{4}$$

$$p(Y|X) = \left(\frac{3}{4}\right)^5$$

Siblings unaffected both parents carrier

$$p(X|Y) = 0.11$$

$$p(\text{next}) = p(X|Y) \cdot \frac{1}{4}$$

Solve for $p(X|Y)$ $p(X) = \frac{1}{3} = \frac{1}{2} \cdot \frac{1}{3}$

$$p(Y|\bar{X}) = 1$$

$$P(\bar{X}) = \frac{2}{3}$$

Lod $\log_{10} \left(\frac{p(\text{unlinked})}{p(\text{linked})} \right)$ $Lod_{\theta} = \log_{10} \left(\frac{\theta^R \cdot (1-\theta)^{NR}}{(1/2)^{total}} \right)$

• F1, where phase parent is unknown \rightarrow

$$Lod = \frac{1}{2} (p(\text{phase 1})) + \frac{1}{2} p(\text{phase 2})$$

\rightarrow Add Lods together for generations.

\rightarrow In F2 we will know phase of parent

Quick Lod = +0.3 for informative, one time pretty -0.3 for unknown phase

need >3 to link linkage

For a part - random A/B placement

A	B	b	B	b	b	B
A	B	b	b	B	B	b
a	b	B	B	b	B	b
a	b	B	b	B	b	B

PD NPD T
 Choices for gametes

1:4:1 for unlinked

Mapping

PD } results probs on second (first is all T)
 NPD }
 TT }
 TT } crossover

Total double = 4 # NPD → 4 recomb
 T Tetrads from double = 2 # NPD
 Total single = T Tetrads - 2 # NPD → 2 recomb
 Don't double count tetrads from double!

$$\text{Distance} = 100 \times \frac{2(T - 2NPD) + 4(4NPD)}{4 \# \text{Tetrads}} = 100 \cdot \frac{T + 6NPD}{2T}$$

We can also apply this to experiment to count # spores of each type, determine linkage

LOD

Given pedigree and genotypes, consider linkage b/w SSRs and traits

$$P(X|Y) = \frac{P(Y|X) \cdot P(X)}{P(Y)} \quad \text{SSR}(A, \theta) \text{ w/ D/A}$$

$$\frac{P(X|Y)}{P(\bar{X}|Y)} = \frac{P(Y|X)}{P(Y|\bar{X})} \cdot \frac{P(X)}{P(\bar{X})}$$

Posterior odds = odds ratio · prior odds

X = linked
 \bar{X} = not linked
 Y = data

If $p > 0.95$, post. odds = 220/1
 prior odds = 1/50
 odds must = 1000

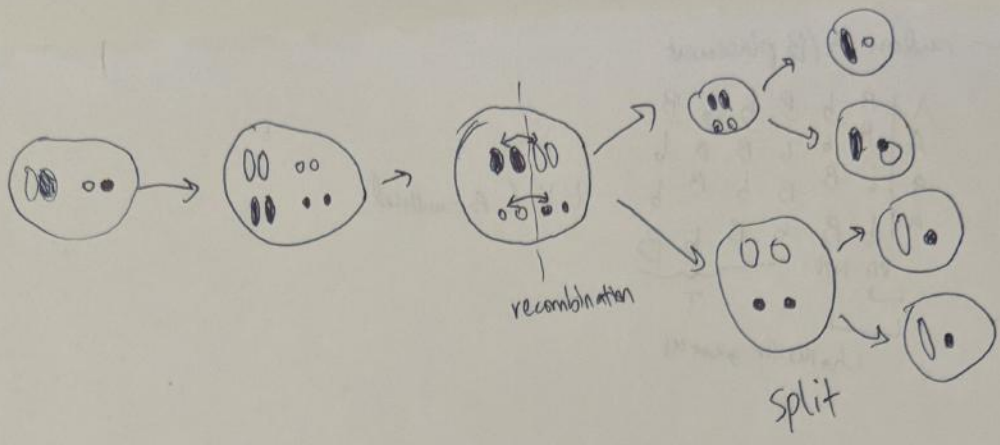
Ex $\frac{DA}{+A}$

LOD = \log_{10} (odds ratio) should be > 3 for significance

Y|X → Assume that $\frac{DA}{+A}$

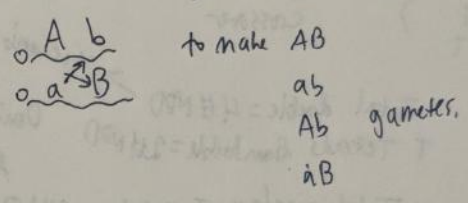
Y| \bar{X} → Assume that $\frac{D+}{+} \frac{A}{B}$ Find probs for D/A, A/B separately

$$P(\text{data} | X) = \frac{1}{2} (p | \text{phase 1}) + \frac{1}{2} (p | \text{phase 2})$$



- unlinked
 - #parentals = #recombs
- weakly linked
 - #parentals > #recombs
- tightly linked
 - #parentals >>> #recombs

To look at recombination, test with heterozygotes, and cross with a wt or recessive homozygote. Then, look at all combinations of gametes to form diploids.



$$\text{Map Distance (genetic distance)} = 100 \cdot \frac{\# \text{recombs}}{\# \text{gametes}} \quad (\text{cM})$$

Mapping function: relationship b/w physical distance (#crossovers) + ^{genetic} distance

→ Identifying SSRs or markers related to ^{mutant} traits of interest

- Get the heterozygote like $\frac{wg^- A}{wg^+ B}$
 - alleles
 - ↑
 - differs

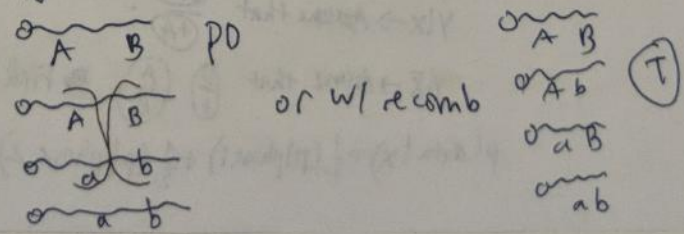
- Cross with recessive homozygote, count the # of each genotype $wg^- A, wg^+ A, wg^- B, wg^+ B$ received from parent by looking at progeny

- 3 factor crosses can account for double recombs
 - 8 possible genotypes, 4 reciprocal pairs
 - the rare class is product of double crossover, so try diff alignments to see what products result

→ Tetrad Analysis: Distance = f(Tetrad types)

2 haploid → diploid → meiosis → 4 gametes

$$\frac{AB}{ab} \times \frac{AB}{ab} =$$



For tightly linked, this is what we have bc double recombs are rare.

$$\text{Dist} = 100 \cdot \frac{\sum I}{2 \sum}$$

Transposon Mutagenesis

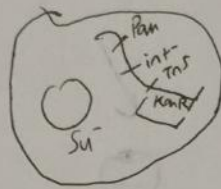
λ -phage - bacterial virus $\left\{ \begin{array}{l} \rightarrow P \text{ gene (replication)} \\ \rightarrow \text{Int gene - Integrating gene (into bacterial genome)} \end{array} \right.$

• Infect Su^- bacteria w/ λ Pam $\text{int}^-::\text{Tn5}$ Su^+ would be able to suppress P_{am} mutation

\downarrow P has nonsense \rightarrow can't integrate

\downarrow contains Tn5 transposon w/ kan^R gene

- Select for Kan^R



Situation:

- \rightarrow can't replicate virus
- \rightarrow can't integrate into bacterial genome
- \rightarrow we need Tn5 to jump into genome

Transposons can put Kan^R or other virus transcribed genes into bacterial DNA

Ways to transfer DNA b/w bacteria:

- ① Transduction: transfer of DNA via bacteriophage
 - ② Conjugation: unidirectional transfer via direct contact
- $F^+ / F' / Hfr \rightarrow F^-$

③ Transformation

① TRANSDUCTION: infects, replicates

P1 phage \rightarrow infect host, replicate DNA + package, lyses cell

$\frac{1}{300}$ of these will mistakenly have *E. coli* genomic DNA

\downarrow when in recipient, DNA from donor can recombine w/ homologous regions

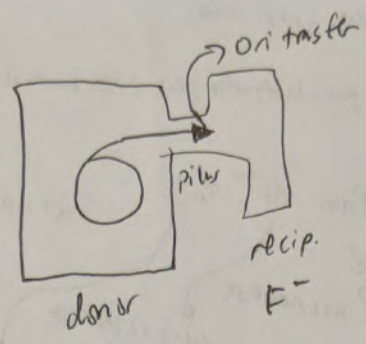
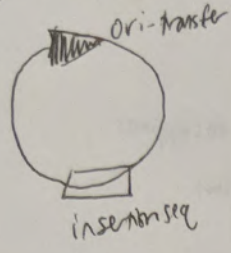
\downarrow recipient acquires donor sequence

- Steps:
- 1) infect strain that has Tn5, collect lysate (virus)
 - 2) infect WT strain (w/o Tn5)
 - 3) select for Kan^R

Donor + recipient genotypes are different to track changes!

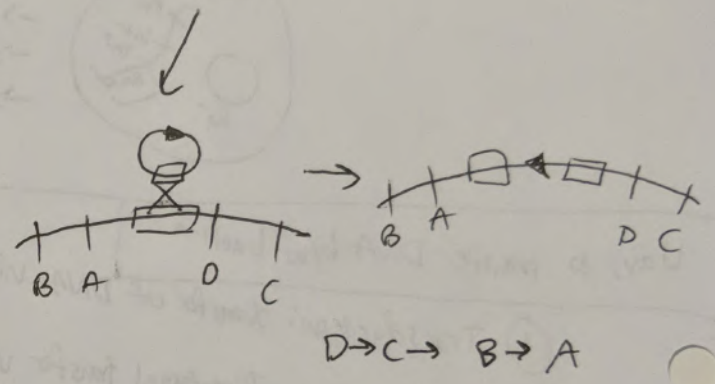
$\text{cotrans } f = \frac{\# \text{ w/ } \text{phenotype}}{\# \text{ resistant}}, \uparrow \text{ freq} = \uparrow \text{ closer}$

Conjugation - F-plasmid



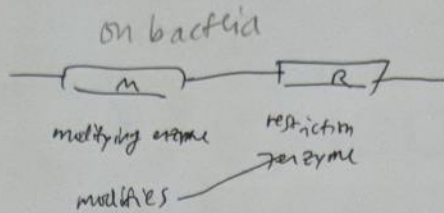
cell containing free F-plasmid

Hfr-cell w/ F-plasmid integrated into genome



Transformation

R plasmid



M+ R⁻, modifies no cut
 M- R⁺ everything cut, bacteria doesn't survive

Clone a gene

Find a specific protein

Generating a library: E. coli, restriction enzyme, mix ligate w/ plasmids, select

- 1) Library generate from mutant into plasmids
- 2) Transform a WT strain w/ plasmids, select
- 3) Lyse open the ones selected for to identify gene

Counting

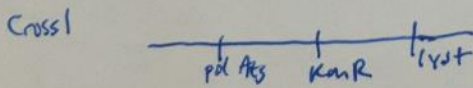
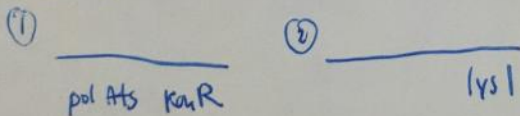
$$P(\text{random stop codon}) = 3/64$$

$$\text{codons} \cdot P(\text{stop}) = \# \text{ random stop codons} = \# \text{ ORFs}$$

$$P(\text{ORF long enough}) = \left(\frac{\# \text{ codons}}{61/64} \right)^{\text{length}}$$

Random for fruitus genes $\rightarrow \# \text{ ORFs} \cdot P(\text{ORF long enough}) \cdot 6$

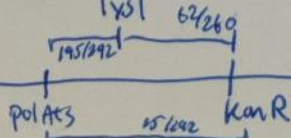
Cotransduction



Get lys⁺ w/ ...



Get pol⁺ w/ ...



Select lys⁺:
 183/260 have polA^{ts}
 62 got KanR

Freqs
 KanR, Lys 62/260
 polA^{ts} - Lys 183/260

Select pol⁺
 97/292 lys⁺
 277/292 KanR

pol⁺ w/ lys⁺: 175/292
 pol⁺ + KanR: 15/292
 \hookrightarrow V for

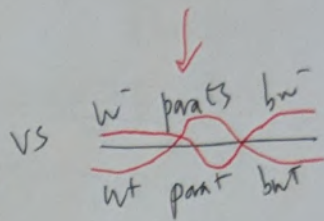
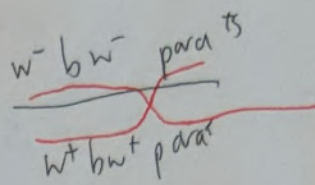
3-factor cross

P ♂ $w^- bw^- para^+$ × ♀ $w^- bw^- para^+$

↓

F1 ♂ $w^- bw^- para^+$ / Y × ♀ $w^- bw^- para^+$ / $w^+ bw^+ para^+$

$w^- bw^- para^+$	65
$w^- bw^- para^+$	4 ← double
$w^+ bw^+ para^+$	4 ← double
$w^+ bw^+ para^+$	71
$w^- bw^+ para^+$	6
$w^- bw^+ para^+$	23
$w^+ bw^- para^+$	20
$w^+ bw^- para^+$	7
<hr/>	
Total	200



Dist $w, para = \frac{8+43}{200} = 25.5 \text{ cM}$

Dist $para, bw = \frac{8+13}{200} = 10.5 \text{ cM}$

If middle int considered
Dist $w, bw = \frac{43+13}{200} = 28 \text{ cM}$

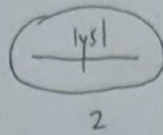
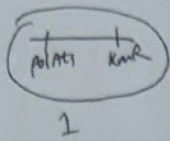
If considered 36 cM

LOD score

$P(\text{data} | \text{completely linked}) \frac{DA}{+B}$

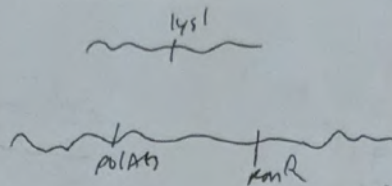
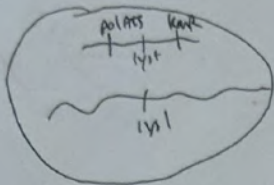
$P(\text{data} | \text{loci unlinked})$

Cotransduction



① Infect 2 w/ phage.
Infect 2.

② Infect 2 w/ phage.
Infect 1.



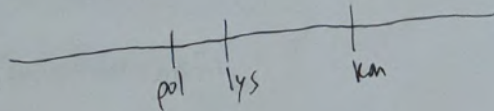
$pol^+ lys^+ = 97/292$
 $pol^+ kan^R = 277/292$
 $polA^S lys = 195/292$
 $polA^S kan^R = 15/292$

$lys + polA^S = 183/260$
 $lys + kan^R = 198/260$
 $lys kan^R = 62/260$

Cotrans free

- ②
- pol & lys : 67%
 - pol & kan^R : 5%

- ①
- lys kan : 24%
 - lys polA^S : 67%



3.4

HW

$f(A/a) = 600 \rightarrow 0.12$
 $f(A/a) = 2000 \rightarrow 0.4$
 $f(A/A) = 2400 \rightarrow 0.48$
 $p = f(A/A) + \frac{1}{2} f(A/a) = 0.48 + 0.2 = 0.68$

$q = f(a) = 0.32$

$H_0 \rightarrow$ in HWE
 $H_1 \rightarrow$ not in HWE

Exp

$f(a/a) = q^2 = 0.1024 \Rightarrow 512$
 $f(A/a) = 2pq = 0.4352 \Rightarrow 2176$
 $f(A/A) = p^2 = 0.4624 \Rightarrow 2312$

$\chi^2 = \sum \frac{(o-e)^2}{e} = \frac{(2312-2400)^2}{2312} + \frac{(2176-2000)^2}{2176} + \frac{(600-512)^2}{512}$
 $= 32.71, p < 0.005, \text{ reject } H_0.$

Selection

Genotype	Freq	Freq after	Δ
A/A	p^2	p^2	0
A/a	$2pq$	$2p(1-s')$	$-2qs'$
a/a	q^2	$q^2(1-s)$	$-q^2s$

$$\Delta q_{sel} + \Delta q_{mut} = 0$$

$$\frac{1}{2}(-2qs') - q^2s + \mu = 0$$

$$\mu = qs' + q^2s$$

Linkage

Controls
 $A1 = 0.9$
 $A2 = 0.1$
 $B1 = 0.5$
 $B2 = 0.5$

Cases

	B1	B2
A1	30	90
A2	12	1

$$D = P_{AB} P_{ab} - P_{Ab} P_{aB}$$

$$= -0.059$$

$$D_{min} = \max \left\{ -P_{Ab} P_{aB}, -q_a q_b \right\}$$

$$= \max \left\{ -\frac{120}{133} \cdot \frac{42}{133}, -\frac{13 \cdot 91}{133^2} \right\} = -0.0668$$

$$P(A1/B1) = \frac{30}{133}$$

$$P(A2/B2) = \frac{1}{133}$$

$$P(A1/B2) = \frac{90}{133}$$

$$P(A2/B1) = \frac{12}{133}$$

$$P(A1) = \frac{120}{133}$$

$$P(B1) = \frac{42}{133}$$

$$P(A2) = \frac{13}{133}$$

$$P(B2) = \frac{91}{133}$$

$$D_{max} = \min \left\{ \frac{120}{133} \cdot \frac{91}{133}, \frac{42 \cdot 13}{133^2} \right\} = 0.0309$$

$$D' = \frac{-0.059}{-0.0668} = 0.883$$

allele correlation: $r^2 = \frac{D^2}{D_{max} D_{min}} = 0.828$

If r (recomb rate) = 0.3

$$D_5 = (1-r)^5 \cdot (-0.059) = -0.0099$$

Odds Ratio

	SPD	Healthy
C	6213	14002
T	120	1054

$$\text{Odds ratio}_{C,SPD} = \frac{(PPI w/ C \text{ and SPD})(PPI w/ T \text{ \& no})}{(PPI w/ T \text{ and SPD})(PPI w/ C \text{ \& no})}$$

$$= 3.897$$

more likely

(b) \rightarrow Measured 10^5 SNPs

$$p' = \frac{0.05}{10^5} = 5 \cdot 10^{-7}$$

prev p-value is still under threshold.

SNP & SPD are...
 H_0 - not asso
 H_1 - assoc

$$\chi^2 = \frac{(ad-bc)^2}{(a+b)(c+d)(a+c)(b+d)} > 224.02 \text{ df} = 1$$

$\rightarrow p < 0.005$

\rightarrow reject H_0 . They are assoc

freq of allele
 $p = f(A), q = f(a) \quad p+q=1$
 $f(A/a) + f(A/a) + f(a/a) = 1$

$p = f(A/A) + \frac{1}{2} f(A/a)$
 freq of genotype

$q = \frac{1}{2} f(A/a) + f(a/a)$

By random mating:
 $f(A/A) = p^2$
 $f(A/a) = 2pq$
 $f(a/a) = q^2$
 $P_i = p_i^2$

w/ rare alleles
 $q \ll 1 \rightarrow p \approx 1$
 $f(A/A) \approx 1$
 $f(A/a) \approx 2q$
 $f(a/a) \approx q^2$
 pop of alleles in heterozygote = $\frac{2q^2}{2q} = q$

- Hw Assumption:
- 1) Random Mating (not assortative)
 - 2) No new mutations
 - 3) No selection
 - 4) No genetic drift / founder effect (pop size)
 - 5) No migration b/w diff pops

χ^2 to obtain P_{exp} , q_{exp} from experimental data (df=1)
 - calc random Hw expected $p^2, 2pq, q^2$
 $\chi^2 = \sum \frac{(O-E)^2}{E}$, df = # classes - # est params - 1

Inbreeding:
 • increasing # homozygotes
 • affects auto recessive #
 $F =$ inbreeding coeff = $\sum p_i^2$ (homozygous)
 Δq inbreeding = $-5Fq$
 prob of someone affected by ~~recessive~~ disease who inbreed $\rightarrow Fq$
 Ex: $f(\frac{a}{a}) = \frac{1}{8}$ inbred (Fq) + $\frac{7}{8}$ not inbred (q^2)

Mutation & Selection



$\Delta q_{mut} = \mu \cdot p = \mu$ if $p=1$
 $S =$ selective disadvantage (0 no eff, 1 all die)

$f = t-s$

$\Delta f_{sel} + \Delta f_{mut} = 0$
 $\Delta q_{sel} + \Delta q_{mut} = 0$

Alternatives:
 Δq_{sel} inbreeding
 Δq_{sel} not inbred
 $\Delta q_{mut} = 0$

Δq_{sel} against homozygotes from random mating + Δq_{sel} against homozygotes from inbreeding + Δq_{mut}
 $\Delta q_{sel} = -Sq^2 + hq + \mu = 0$
 $\rightarrow q =$ steady state q

Ex: mutations at $10^{-6} = \mu$
 $s = 0.9, h = 0.03$
 steady state

$F = 1/8$, inbred = 1.5%
 $0 = \mu + (-Sq^2)0.85 + 0.15(-5Fq)$
 steady state q

Genotype	f	f after	Δf
AA	p^2	p^2	
Aa	$2pq$	$2pq(1-h)$	$-2hq$
aa	q^2	$q^2(1-s)$	$-Sq^2$

$\Delta q_{sel} = \Delta f(\frac{a}{a}) + \frac{1}{2} \Delta f(\frac{A}{a}) = -Sq^2 + \frac{1}{2}(2hq)(-h)$
 $q = h/s$

Recessive
 $-q^2s + \mu = 0 \quad q = \sqrt{\frac{\mu}{s}}$
 Dom: $-\frac{1}{2}(2sq) + \mu = 0$
 $\mu = Sq$

Haplotype: $\frac{A}{a} \frac{b}{b}$ LE expected $\Rightarrow p(AB) = p(A)p(B)$ etc
~~MAA~~ LE estimated $\Rightarrow p_A = p_{AB} + p_{Ab}$ etc

LE \rightarrow LD
 - pop ad mixture
 - founder effect
 - selection

$D = P_{AB} \cdot P_{ab} - P_{Ab} \cdot P_{aB}$
 $D_{min} = \max\{-P_{Ab}P_{aB}, -P_{AB}P_{ab}\}$
 $D_{max} = \min\{P_{AB}P_{ab}, P_{Ab}P_{aB}\}$
 $D' = \begin{cases} D/D_{min} & D < 0 \\ D/D_{max} & D > 0 \end{cases}$

$r^2 = \frac{D^2}{P_A P_a P_B P_b}$
 $P_{AB}^{(n)} = (1-r)P_{AB} + rP_A P_B$, $r =$ recomb rate
 $D_n = (1-r)^n D_0$
 $r = 0.5 \Rightarrow$ unlinked

Brother-sister Mating
 $F = 1/4$

1st Cousins
 $F = 1/16$

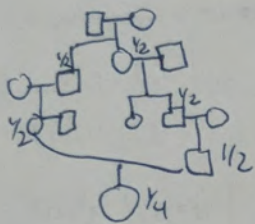
Ex) Consider autosomal recessive trait present in $1/250000$ newborns. b/B .

$$f(b) \Rightarrow b^2 = \frac{1}{250000}, b = \frac{1}{500}$$

- homozygotes have 90% as many offspring as others.
what is μ for ss ?

$$\text{recessive} \rightarrow -Sq^2, \mu = 0, s = 0.1, a = b$$

- consider effect of a change in mating patterns if every person mates w/ cousin of one of their parents.
Frequency of recessive trait in 1st generation after?
 $s=0, h=0$



$$4 \left(\frac{1}{2}\right)^2 = F \quad \underline{f(bb) = Fq}$$

$$f(N) = 0.0505$$

↓
put into situation where $S=0.9$, for dominant disease

$$\Delta q = -qS = -0.9 \cdot 0.0505$$

$$\downarrow$$

$$\frac{1}{2}(-2qS)$$

$$f(N)_{\text{final}} - f(N)_{\text{init}} = -0.9 \cdot 0.0505$$

GWAS

- Case/control

- case-sectional (once in time)
- cohort longitudinal - collected over time
- case-cohort - look at cases/controls in specific group/pop

Observed:

	Cases	Controls	Total
A0	a	b	a+b
A1	c	d	c+d
Total	a+c	b+d	a+b+c+d

$$OR(A0) = \frac{(w/\text{disease}, A0)(w/\text{no disease}, A1)}{(w/\text{no disease}, A0)(w/\text{disease}, A1)}$$

H_0 - not assoc

H_1 - assoc

↑ OR, more corr.

Est

	Cases	Controls
A0	$\frac{(a+b)(a+c)}{N}$..
A1

Significance of OR ↓

$$\chi^2 = \frac{(ad-bc)^2(a+b+c+d)}{(a+b)(c+d)(a+c)(b+d)}, df=1$$

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$$\chi^2 = \sum \frac{(O_i - E_i)^2}{E_i}$$

- 1 est case freq
- 1 allele freq

If $p < \text{threshold}$:

- reject null hypothesis
- also χ^2 is high

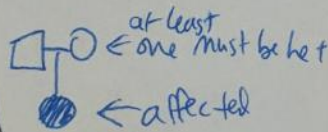
$p > \text{threshold}$

- accept (don't reject) null hypothesis
- χ^2 is low → matches up w/ expected

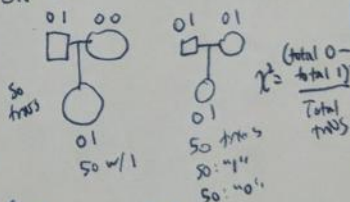
TRIOS

$$\chi^2_{TRIO} = \frac{(n_1 - n_2)^2}{(n_1 + n_2)}$$

H_0 alleles transmitted 1:1
 H_A preferential transmission



Ex 250 trios



*Count for each trio # times an allele was passed down from a het parent

$$\bar{x} = \frac{\sum f_i x_i}{N}$$

in class, Val of class

$$Var s^2 = \frac{\sum f_i (x_i - \bar{x})^2}{N-1}$$

s , standard dev = $\sqrt{s^2}$

$$\sigma_p^2 = \sigma_g^2 + \sigma_e^2$$

Broad sense heritability

$$H^2 = \frac{\sigma_g^2}{\sigma_p^2} = \frac{\sigma_g^2}{\sigma_g^2 + \sigma_e^2}$$

Narrow Sense: ratio of additive genetic var to total phenotypic diff

$$h^2 = \frac{M^* - M}{M^* - M}$$

M = Mean, parent gen
 M^* = mean parents selected
 M' = Mean, progeny

Multi Hypothesis Correction

decision	H_0 not rejs	H_0 rejs
H_0 true	truly null	false pos I
H_0 false	false negative II	truly alt

*p-value = probability (Type I error) (α)

~~*Power~~

*Power = 1 - prob we made Type II error = 1 - β

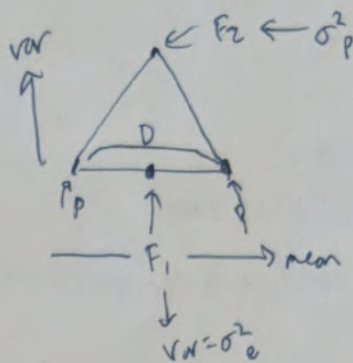
*Control: prob of making at least 1 Type I error in a family of tests

Now $\rightarrow P(A_i) \leq \alpha/N$
 p-value for N tests each test

Covariance b/w pairs of relatives

$$\text{Cov}(x, y) = \frac{\sum f_i (x_i - \bar{x})(y_i - \bar{y})}{N-1}$$

$$r = (\text{in correlation coeff}) = \frac{\text{Cov}(x, y)}{s_x s_y}$$



$$r = \frac{D^2}{8\sigma_g^2}$$

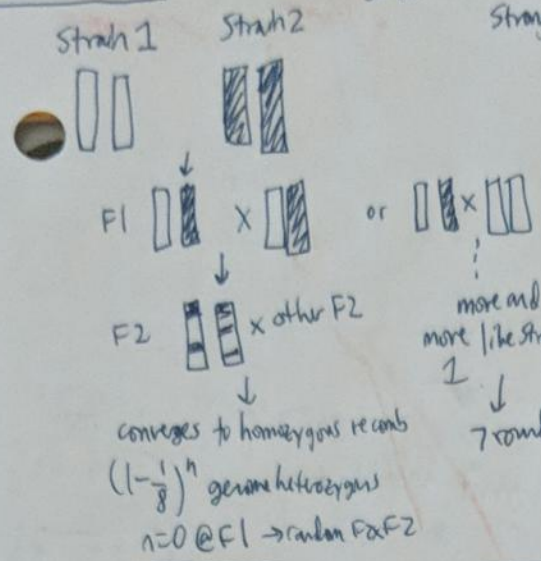
Ex - monozygotic twins $\rightarrow r = H^2$, $\sigma_p^2 \approx \sigma_e^2$

↑
corr.
coeff.

Ex. Full siblings $r = \frac{H^2}{2}$

Exam #2

QTL - minor contributors over major ones
 Strong phenotype x strain w/o phenotype
 P1 backcross 2 gen

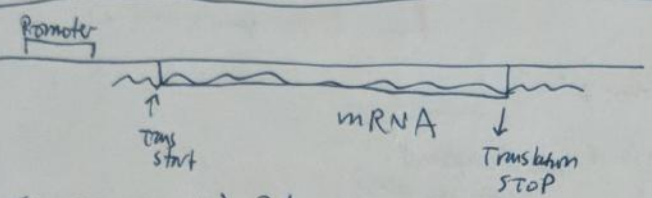


Transposon - can confer resistance into bacteria like Tn5-KanR

For E. coli, use λ phage

λ Pam int⁻ Tn5
 Su⁺ - suppress Pam
 Su⁻ - only way to get KanR is to jump
 • P replication Pam = amber mutation in replication
 • Int integration int⁻ - can't integrate into bacterial genome

Strategy: Infect E. coli w/ λ Pam int⁻ Tn5
 select for KanR
 These have Tn5 put in randomly somewhere
 *Identifying where gene A is
 This can knock out A if Tn5 jumps into middle of it.



Gen seq - $p(\text{stop codon}) = 3/64$
 $\# \text{ORFs (length } \geq k) = \frac{1}{3} \cdot (p(\text{not stop}))^k \cdot \# \text{total ORFs} \cdot b$
 $p(\text{ORF} \geq k) = (p(\text{not stop}))^k$
 $\# \text{total ORFs} = \# \text{codons in genome} \cdot p(\text{stop}) = \# \text{random stops}$

Mutations

- Missense: base change
- Nonsense: codon \rightarrow stop (via base change)
- Frameshift: indel
- Screen - identifying an altered prop
- selection - parent strain culture, desired mutant can
- Base Analog - something inserted, interpreted as one thing, can bond to another
- Base-Modifying - chemical damage - repairs hard errors
- DNA - intercalator - \square b/w bases - miscopying by polymerase

Suppressors: revertants - mutants that reverse effect of primary mutation

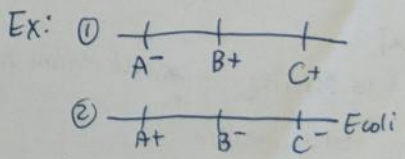
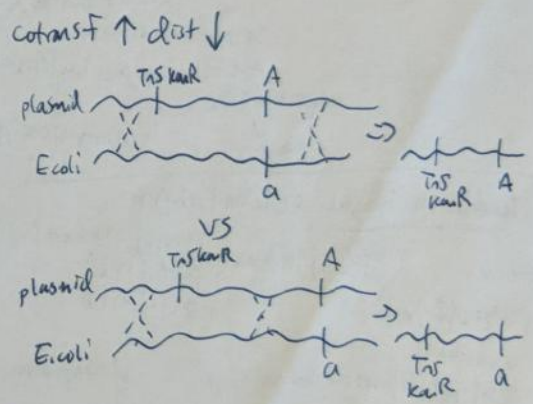
- 1) Back mutation
- 2) Intragenic - mutation in same gene
- 3) Extragenic - compensating mutation in diff gene
 \hookrightarrow Nonsense suppressors (like Am suppressor Su⁺)
 \downarrow
 holes via mutations to tRNA (codon is right, but attached AA isn't)

PCR

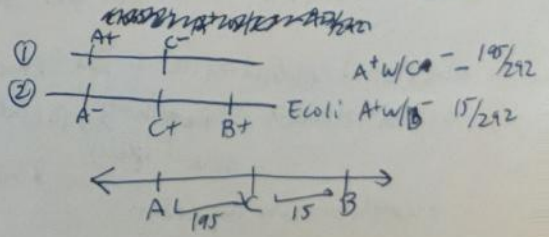
TRANSDUCTION

- 1) infect strain that has Tn5, collect virus
- 2) infect WT strain (or other strain)
 \rightarrow observe recombinations
- 3) select for trait
- 4) screen for phenotype

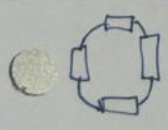
$\text{cotransf b/w} = \frac{\# \text{w/ trait 2}}{\# \text{selected w/ trait 1}}$



Cross 1: $C^+ A^- = 183/260 \rightarrow$ stuff from plasmid!
 $C^- B^+ = 62/260$

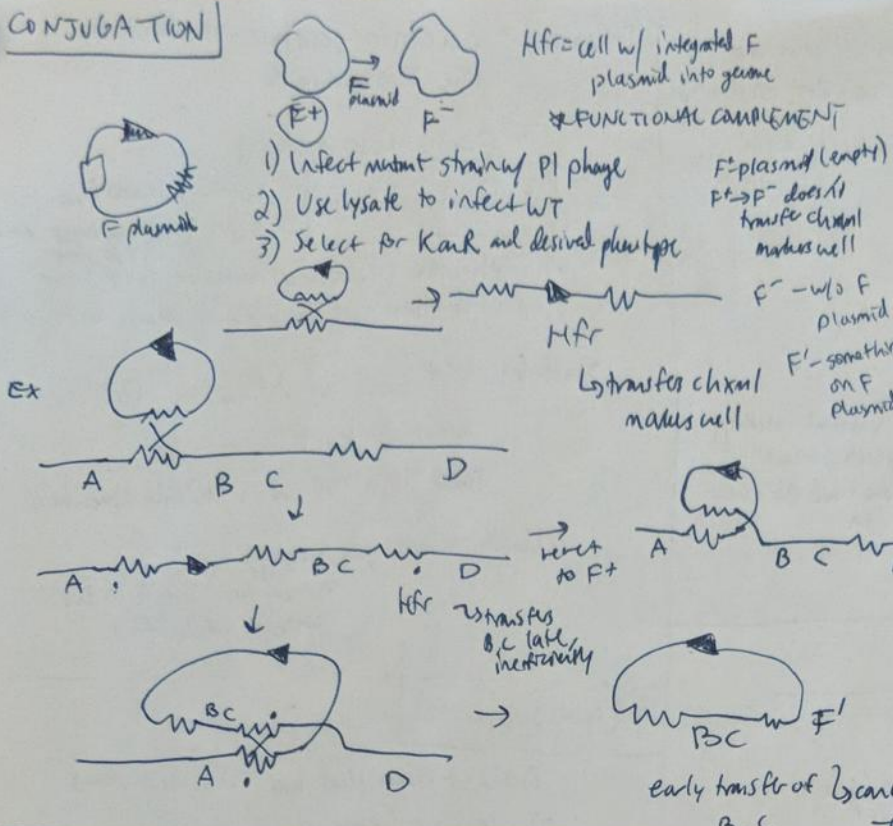


Transformation



M⁺R⁻ - modifies, doesn't cut any phage
 M⁻R⁺ - everything it cut in, bacteria
 Generate a library - E. coli, restriction enzyme, mix w/ set of plasmids, select
 1) Library generate from mutant into plasmids, select
 2) transform a WT strain w/ plasmid, select
 3) Lysate open one that you want
 \hookrightarrow Clone a gene? \rightarrow Find a gene?

CONJUGATION



PSET 3.4: back mutation as suppressor?

trp^- or trp^+ w/ trp^+/his^-
 arg^3 or arg^3 w/ gal^2

Transduct & into X.
 Select w/ lysine.
 Are all resulting bacteria WT w/ respect to trp ? or no?
 back m Extragenic suppression

Needleman Wunsch: Global align

$space = mn$
 $complexity = O(2^{k-1}mn)$
 $k = \# sequences$
 2^{k-1} refers to boxes checked per step $d = gap pen.$

$F(i,j) = \max \begin{cases} F(i-1, j-1) + score(i,j) \\ F(i-1, j) + d \\ F(i, j-1) + d \end{cases}$ $F(0,0) = 0$
 $F(i,0) = d \cdot i$
 $F(0,j) = d \cdot j$

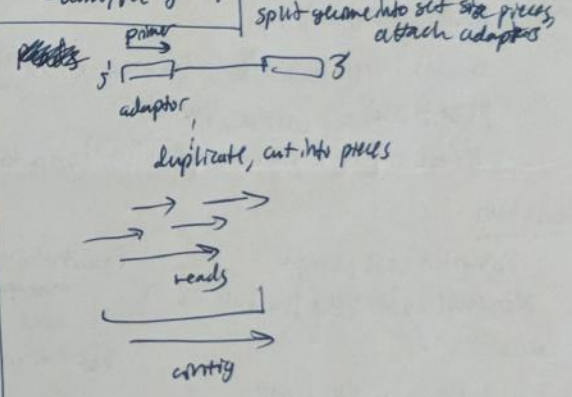
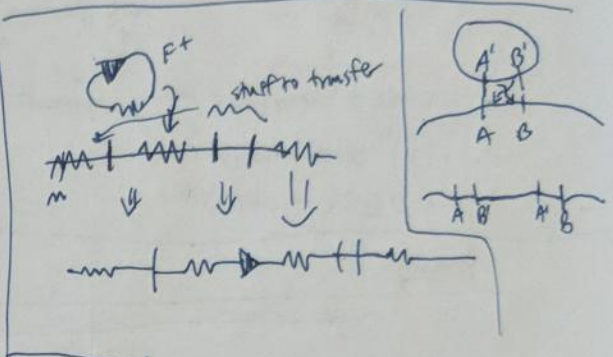
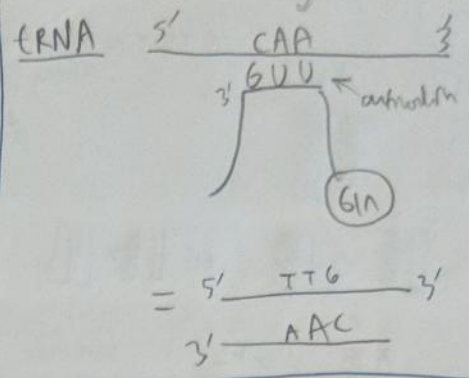
Smith Waterman: Local

add 0 to $F(i,j)$ eg conserved regions via evolution

SIMILARITY
 DISSIMILARITY

Dot plots to identify differences - simplify for

- * In exons: conserved regions + low base changes (nonsyn)
- * In introns/exons: frameshifts, gaps (indels), etc among related species
- * indels are clean when $\neq 3 AA$
- * watch for early stop codons



EX. C G A T C T T A A G C C T T A T A

These 2 are a real pair

paired end reads help us determine k/w

repetitive elements paired

